

Optimization of Design Complexity in Time-Multiplexed Constant Multiplications

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Abstract—The multiplication of constants by a data input is an essential operation in digital signal processing (DSP) systems. For applications requiring a large number of constant multiplications under stringent hardware constraints, it is generally realized under a folded architecture, where a single constant selected from a set of multiple constants is multiplied by the data input at each time, called time-multiplexed constant multiplication (TMCM). This paper addresses the problem of optimizing the complexity of a TMCM design and introduces an algorithm that finds the least complex TMCM design by sharing the logic operators, *i.e.*, adders, subtractors, adders/subtractors, and multiplexers (MUXes). It includes efficient search methods, yielding better results than existing TMCM algorithms.

I. INTRODUCTION

The multiple constant multiplications (MCM) operation, realizing the multiplication of constants by an input variable, dominates the design complexity of many DSP systems. Since these constants are determined beforehand, the constant multiplications are generally replaced with addition, subtraction, and shift operations. In hardware, shifts can be realized using only wires without representing any cost. Over the years, efficient algorithms were proposed for the optimization of the number of adders and subtractors in the MCM operation [1]–[3].

However, as the number and size of the constants increase, the increase in complexity is inevitable if the constant multiplications are realized simultaneously in a parallel architecture. Hence, in DSP applications targeting low complexity, a folded architecture [4] is preferred, where the common resources are allowed to be shared in time, taking into account an increase in latency. In folded design of DSP systems, TMCM is a fundamental operation. Given a set of n constants, its straightforward realization, the *mux-mul* architecture, includes a generic multiplier and an n -to-1 MUX, where i denotes the select input with $0 \leq i \leq n-1$ (Fig. 1a). Another realization, the *mcm-mux* architecture, uses an n -to-1 MUX and an MCM block including adders and subtractors that implement the constant multiplications (Fig. 1b). An alternative solution, the *mux-add* architecture, includes adders, subtractors, and adders/subtractors (determined by a select input) with MUXes (Fig. 1c). It increases the number of constants that a logic operator can generate and provides the possible sharing of logic operators. Hence, it may yield less complex TMCM designs when compared to other architectures [5]–[10].

The single-input single-output (SISO) and single-input multiple-output (SIMO) TMCM blocks occur in folded design of filters and filter banks, respectively [8]. In this work, the constants of a TMCM operation are represented in an $m \times n$ matrix C , where m and n are the number of outputs and time slots (the number of constants in an array), respectively. Thus,

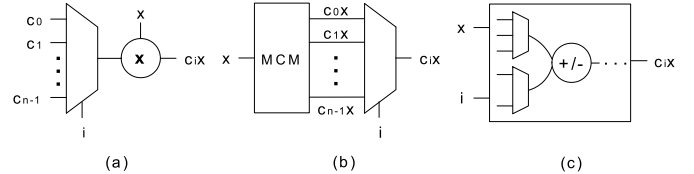


Fig. 1. TMCM architectures: (a) *mux-mul*; (b) *mcm-mux*; (c) *mux-add*.

given C , the *TMCM problem* is defined as finding a set of logic operators, *i.e.*, adders, subtractors, adders/subtractors, and MUXes, that realizes the TMCM operation and leads to a TMCM design with minimum complexity. Existing methods targeting the *mux-add* architecture consider different design platforms, *i.e.*, application specific integrated circuits (ASIC) and field programmable gate arrays. They reduce the complexity of a TMCM operation by sharing the basic structures and merging the single/multiple constant multiplication graphs. The exact method [5] can only be applied to a small number of constants and the solution quality of the approximate methods [6]–[10] depends heavily on the TMCM instance.

This paper introduces our TMCM algorithm ORPHEUS that targets the *mux-add* architecture and the SIMO TMCM operations under an ASIC design platform, where the area values of logic operators are taken from a standard cell library. It includes two main parts: optimal and heuristic. In its optimal part, the arrays of constants, that can be realized using a single logic operator, are synthesized. In its heuristic part, an array of constants is chosen, its alternative implementations are found, and it is synthesized with the one that has the smallest cost. ORPHEUS iterates until all arrays of constants are synthesized.

II. ORPHEUS: A TMCM ALGORITHM

The steps of ORPHEUS, that will be described more briefly in the next subsections, are given below. In these steps, the set M , that initially consists of an input variable denoted by 1, will include constants whose multiplications by the input variable will be found by the MCM algorithm [3]. Also, the matrix S , that initially consists of a single array of n 1s, will include the synthesized arrays of constants. Note that the input variable(s) is (are) always available. The set I will include logic operators realizing the TMCM operation.

- 1) Given the constant matrix of the TMCM operation C , determine the non-redundant target matrix T .
- 2) In an iterative manner, find an optimal realization of a row of T , T_i , if it exists, remove T_i from T to S , update M if necessary, and add this realization to I .
- 3) If T is empty, go to Step 10.
- 4) Select an array of constants from T , T_i .
- 5) Find a realization of T_i using a single operation whose one of inputs is a row of S or its shifted version and that has the smallest estimated cost value $ecost_1$.
- 6) Find a realization of T_i under the *mcm-mux* architecture and compute its estimated cost value $ecost_2$.

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- 7) Find a realization of T_i using a single operation that has the minimum number of distinct partial terms at its inputs and the smallest estimated cost value $ecost_3$.
- 8) Among these three realizations, choose the one with the minimum cost value and update T , S , I , and M .
- 9) If T is not empty, go to Step 2.
- 10) Design the MCM block for the constants of M using the MCM algorithm [3], update and return I .

In following subsections, these steps are described through an example with a 4×2 matrix $C = [5 \ 5; 2 \ 1; 12 \ 10; 92 \ 196]$.

A. Step 1: Preprocessing Phase

The negative constants of C are converted to positive, because it is always assumed that the sign of a constant is handled where the constant multiplication is required using an adder/subtractor. For each row of C , C_i , its left shift, ls_i , is found by dividing C_i by 2 until at least one of its constants is odd and $C_i \cdot 2^{-ls_i}$ is added to T without repetition. For our example, T is obtained as $[5 \ 5; 2 \ 1; 6 \ 5; 23 \ 49]$.

B. Step 2: Finding Optimal Realizations

First, we check each row of T , T_i , if it includes the same constant at its every time slot. If such an array of constants exists, it is removed from T to S and this constant is added to M without repetition. For our example, the row of T , $[5 \ 5]$, is removed from T to S and 5 is added to M .

Second, we check each T_i if its constants are 1 or its shifted versions so that it can be realized using a single MUX. If there exists such an array of constants, it is removed from T to S and this MUX is added to I . For our example, the row of T , $[2 \ 1]$, can be realized using a single MUX.

Third, we check each T_i if it can be realized using a single operation, i.e., an adder, a subtractor, or an adder/subtractor, whose inputs are the rows of S or their shifted versions. While searching such realizations, the array of constants D is computed as follows for each S_j , ls_j , and SM_k :

$$D \cdot 2^{ls_d} = T_i - (S_j \cdot 2^{ls_j}) \star SM_k \quad (1)$$

where $ls_d \geq 0$ denotes the left shift of D , $1 \leq j \leq |S|$, ls_j stands for the left shift of S_j , $0 \leq ls_j \leq mbc(T_i) - mbc(S_j) + 1$ (where $mbc(A)$ function determines the maximum bitwidth of constants in an array A), SM is a $2^n \times n$ sign matrix including all possible signs, i.e., 1 and -1 , for the $1 \times n$ array S_j , and $1 \leq k \leq 2^n$. Note that $\star$ denotes the element-by-element product of arrays, e.g., in $C = A \star B$, each entry in the array C is the product of the corresponding entries in arrays A and B . Thus, if D is equal to a row of S , then T_i can be realized using a single operation. If SM_k includes all 1s, then the operation is an adder. If SM_k includes all -1s, then it is a subtractor. Otherwise, it is an adder/subtractor. If such a realization is found, it is added to I and T_i is removed from T to S . In our example, for the row of T , $[6 \ 5]$, one possible D is found as $[1 \ 1] \cdot 2^2 = [6 \ 5] - ([2 \ 1] \cdot 2^0) \star [1 \ 1]$, which is also a row of S . This realization of $[6 \ 5]$ needs a single adder.

This procedure iterates until there exists no such row of T . For our example, T , S , and M are respectively found as $[23 \ 49]$, $[1 \ 1; 5 \ 5; 2 \ 1; 6 \ 5]$, and $\{1, 5\}$ at the end of this step.

C. Step 4: Selection of an Array of Constants

At this point, there exist array(s) of constants in T which require(s) partial arrays of constants. In each iteration of ORPHEUS, we select one of them that has the minimum

$tnzd$ value, denoting the total number of nonzero digits of constants in an array under the canonical signed digit (CSD) representation¹ [1]. A smaller $tnzd$ value roughly indicates that the array can be realized using less number of logic operators. Hence, this metric is preferred to increase the sharing of logic operators, since ORPHEUS considers the synthesized arrays of constants of S in the realization of a row of T (Steps 2, 5, and 7). It is also used to ensure the convergence of each realization to an array consisting of 1 or its shifted versions (Step 5).

D. Step 5: First Alternative Realization

Possible realizations of a row of T , T_i , are found based on the computation in Eqn. 1. To avoid the exponential number of sign values for the constants of S_j , we traverse each constant, $S_j[h]$ with $1 \leq h \leq n$, compute $D[h]$ for both sign of $S_j[h]$, i.e., 1 and -1 , and choose the one that leads to $D[h]$ with minimum number of nonzero digits under CSD. After D and the sign array, corresponding to SM_k in Eqn. 1, are determined, we check if the $tnzd$ value of D is less than that of T_i to ensure the convergence of D . If so, the type of operation is determined as done in Step 2 and its cost in a given standard cell library, $cost_{op}$, is found [9]. We also estimate the cost of D as if it will be realized under the *mcm-mux* architecture. First, the different constants of D and its quantity, i.e., r , are found. If $r > 1$, the cost of an r -to-1 MUX in a given standard cell library, $cost_{mux}$, is found [9]. Otherwise, it is set to 0. Second, we convert each constant of D to an odd constant, find the minimum number of operations determined by the algorithm [11] required for its multiplication by the input variable, compute the cost values of these operations assuming them as adders, and add them to $cost_{add}$, which was initially set to 0. The $cost_{add}$ value is computed without repeating the same odd constants. Thus, the implementation cost of T_i is found as $cost_{op} + cost_{mux} + cost_{add}$. After all possible realizations of T_i are found considering each S_j with its all possible ls_j values, we choose the one with the minimum cost value that is assigned to $ecost_1$.

For the row of T , $[23 \ 49]$, its realization with the minimum cost is found as $[3 \ 6] \cdot 2^3 + ([1 \ 1] \cdot 2^0) \star [-1 \ 1]$, requiring an adder/subtractor and the partial array of constants $[3 \ 6]$ which is estimated to need a 2-to-1 MUX and an adder.

E. Step 6: Second Alternative Realization

The cost value of the *mcm-mux* realization of T_i is computed as described for the estimation of the cost of D in Step 5, except that the elements of M are considered in this case. If the odd version of a constant of T_i is an element of M , then it is not considered in computation of $cost_{add}$. Thus, $ecost_2$ is found as $cost_{mux} + cost_{add}$. For our example, the estimated cost of $[23 \ 49]$ includes a 2-to-1 MUX and 4 adders.

F. Step 7: Third Alternative Realization

In this realization of T_i , we aim to find an implementation (an adder or a subtractor) for each constant of T_i such that these operations include the minimum number of distinct partial terms at their inputs. The reason behind this is that common partial terms reduce the sizes of MUXes and the number of elements in the partial array of constants. This problem is formalized as a 0-1 integer linear programming (ILP) problem.

First, we find all realizations of each constant of T_i by decomposing its nonzero digits in two partial terms when it

¹An integer can be written in CSD using k digits as $\sum_{j=0}^{k-1} d_j 2^k$, where $d_j \in \{1, 0, \bar{1}\}$ and $\bar{1}$ denotes -1 . The nonzero digits are not adjacent and a constant is represented with minimum number of nonzero digits under CSD.

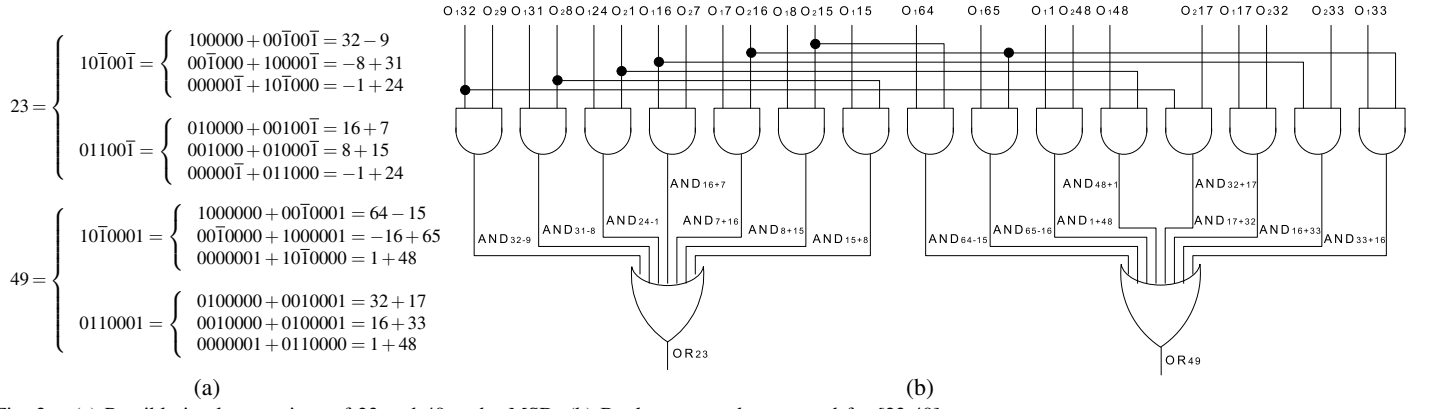


Fig. 2. (a) Possible implementations of 23 and 49 under MSD; (b) Boolean network generated for [23 49].

is defined under the minimal signed digit (MSD) representation² [2]. For the row of T , [23 49], the possible realizations of its constants are given in Fig. 2a. Since a constant may have multiple representations under MSD, the number of possible realizations is increased. But, this may yield similar realizations, e.g., $-1 + 24$ and $48 + 1$ for 23 and 49, respectively.

Second, we represent the realizations of constants in a Boolean network that includes only AND and OR gates. For an adder, two AND gates, denoted as $AND_{p_1+p_2}$ and $AND_{p_2+p_1}$, are generated due to the commutative law of addition. For a subtractor, we assume that the first input is the partial term with the positive sign and the second input is the one with the negative sign and we generate an AND gate denoted as $AND_{p_1-p_2}$. For each constant of T_i , $T_i[h]$, where $1 \leq h \leq n$, an OR gate, $OR_{T_i[h]}$, is generated to combine all realizations of $T_i[h]$. Each partial term p_k at the first or second input of an operation is denoted as an optimization variable, $O_1[p_k]$ or $O_2[p_k]$, respectively. The network generated for the row of T , [23 49], is shown in Fig. 2b.

Third, the objective function of the 0-1 ILP problem is found as a linear combination of optimization variables whose weights are 1. Its constraints are obtained by finding the conjunctive normal form (CNF) formulas of each gate and expressing each clause of the CNF formulas as a linear inequality [12]. For example, a 2-input AND gate, $c = a \wedge b$, is translated to CNF as $(a + \bar{c})(b + \bar{c})(\bar{a} + \bar{b} + c)$ and converted to linear constraints as $a - c \geq 0$, $b - c \geq 0$, $-a - b + c \geq -1$. The outputs of OR gates associated with constants of T_i , $OR_{T_i[h]}$, are set to 1, since they need to be implemented.

Forth, a minimum solution is found using a 0-1 ILP solver and based on the selected operations (the outputs of AND gates set to 1 in the solution), the realization of T_i is formed as:

$$T_i = G_1 \cdot 2^{ls_1} + (G_2 \cdot 2^{ls_2}) \star SA \quad (2)$$

where G_1 (G_2) includes the first (second) inputs of the selected operations for each constant of T_i , ls_1 (ls_2) is the amount of left shift of G_1 (G_2), and SA denotes the sign array and is determined based on the type of each operation, i.e., if $T_i[h]$ is realized using an adder, then $SA[h]$ is 1, otherwise, it is -1. For our example, the operations $7 + 16$ and $65 - 16$ are respectively found for constants 23 and 49, and the realization of [23 49] is obtained as $[7 \ 65] \cdot 2^0 + ([1 \ 1] \cdot 2^4) \star [1 \ -1]$ according to Eqn. 2.

Finally, we compute the cost of this realization as done in Step 5. To do so, we define the type of operation based on

²MSD differs from CSD in one property which allows the nonzero digits to be adjacent. Thus, a constant may have alternative representations in MSD, all including minimum number of nonzero digits.

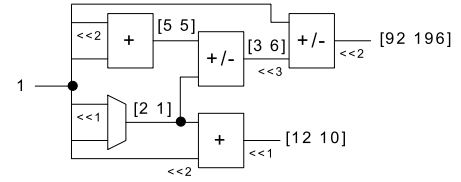


Fig. 3. Time-multiplexed realization of $C = [5 \ 5; 2 \ 1; 12 \ 10; 92 \ 196]$.

SA and compute its cost, $cost_{op}$ [9]. For any of G_1 and G_2 , if it is not included in S , then we estimate its cost in terms of $cost_{mux}$ and $cost_{add}$. For our example, the type of operation is adder/subtractor and only the cost of [7 65] is estimated.

This solution leads to an operation with common partial terms at the inputs. In order to include an information about the design complexity into the 0-1 ILP problem, for each partial term p_k , we also take into account its bitwidth $bw(p_k)$ and number of nonzero digits under CSD $nzd(p_k)$. Hence, we modify the objective function of the previous 0-1 ILP problem, where the weight of each optimization variable, denoting a partial term p_k at the inputs of operations, is assigned to $bw(p_k) \cdot nzd(p_k)$. In this case, 23 and 49 are implemented as $8 + 15$ and $64 - 15$, respectively and the realization of [23 49] is determined as $[1 \ 8] \cdot 2^3 + ([15 \ 15] \cdot 2^0) \star [1 \ -1]$, requiring an adder/subtractor and the partial arrays [1 8] and [15 15].

Among these two possible realizations, we determine the one with the minimum cost which is assigned to $ecost_3$. For our example, the second one has the minimum cost.

G. Step 8: Selection of the Realization with Minimum Cost

Among the realizations found in Steps 5, 6, and 7, if $ecost_1$ is the minimum, we add the required partial array of constants (found in Step 5) to T . If $ecost_2$ is the minimum, we remove T_i from T to S and add the odd versions of constants in T_i to M without repetition. Otherwise, we add the required partial array(s) of constants (found in Step 7) to T . In case of equality of cost values, the realization found in Step 6 is favored first, and then, the one found in Step 5. For our example, $ecost_1$ is the minimum cost value, and thus, [3 6] is added to T .

H. Step 9: Iterations in ORPHEUS

ORPHEUS iterates until T is empty. For our example, in the next iteration, [3 6] and [23 49] are respectively realized as $[5 \ 5] \cdot 2^0 + ([2 \ 1] \cdot 2^0) \star [-1 \ 1]$ and $[3 \ 6] \cdot 2^3 + ([1 \ 1] \cdot 2^0) \star [-1 \ 1]$.

I. Step 10: Realization of the Necessary MCM Block

If M includes constants other than 1, the MCM algorithm of [3] is applied to find the fewest number of operations realizing these constant multiplications and these operations

TABLE I. SUMMARY OF ALGORITHMS ON SISO TCMC INSTANCES.

<i>mbc</i>	<i>n</i>	2	6	10	14	18
6	#BS	27	19	21	24	29
	Min Gain	-4.78	-19.85	-18.19	-16.91	-1.94
	Avg Gain	9.16	4.20	6.75	9.94	17.03
	Max Gain	30.30	31.90	28.98	28.21	32.75
	CPU DAGfusion	0.76	2.90	8.08	11.29	19.34
	CPU ORPHEUS	0.94	0.33	1.07	1.50	2.15
8	#BS	24	16	20	18	26
	Min Gain	-9.46	-13.52	-19.95	-16.14	-7.98
	Avg Gain	8.20	2.93	4.51	5.98	12.71
	Max Gain	25.54	26.02	22.71	25.25	34.46
	CPU DAGfusion	0.84	4.84	11.41	15.55	20.42
	CPU ORPHEUS	1.39	1.75	2.24	2.83	4.19
10	#BS	22	15	16	19	24
	Min Gain	-23.26	-14.75	-12.85	-12.91	-15.97
	Avg Gain	6.99	1.27	0.75	7.59	7.81
	Max Gain	28.48	27.66	22.96	28.51	27.75
	CPU DAGfusion	0.83	7.18	20.97	113.34	99.28
	CPU ORPHEUS	1.94	2.86	3.84	5.55	8.57
12	#BS	25	18	18	24	19
	Min Gain	-12.06	-19.22	-14.69	-21.54	-20.33
	Avg Gain	13.88	3.17	4.17	6.80	4.75
	Max Gain	43.23	39.97	23.96	27.91	24.52
	CPU DAGfusion	1.00	23.54	65.72	276.09	515.20
	CPU ORPHEUS	2.85	4.89	7.12	8.68	13.42

are added to I . Also, for each chosen *mcm-mux* realization, the necessary MUX is added to I . The solution on our example C is given in Fig. 3, where the select inputs of the MUX and adders/subtractors are not shown for the sake of clarity.

III. EXPERIMENTAL RESULTS

This section presents the results of ORPHEUS, comparing them to those of prominent TCMC algorithms. ORPHEUS was written in MATLAB and was run on a PC with Intel Xeon at 2.4GHz and 10GB memory. Note that DAGfusion [9] was obtained from www.spiral.net and its exhaustive search on all possible orderings of SCM graphs was limited to 10,000 orderings, since it may take enormous CPU time.

As the first experiment set, we used randomly generated $1 \times n$ TCMC instances, where the maximum bitwidth of constants (*mbc*) varies in between 6 and 12 in increment of 2 and n ranges between 2 and 18 in increment of 4. For each group, there were 30 instances, a total of 600 instances. Table I presents the results of algorithms, where #BS denotes the number of better solutions that ORPHEUS found against DAGfusion [9] in terms of complexity, computed using the 0.18- μ m standard cell library when the bitwidth of the input variable (*bwi*) was 16. *Min Gain*, *Avg Gain* and *Max Gain* denote the minimum, average, and maximum gain in percentage obtained by ORPHEUS over DAGfusion, respectively. Average runtime of both methods is given in seconds.

Observe from Table I that ORPHEUS obtains better solutions than DAGfusion on more than half of the total number of TCMC instances, *i.e.* 30, in each group, except that including 10-bit 6 constants. Its maximum gain over DAGfusion is greater than 20% on every group of instances, reaching up to 43.23% on a TCMC instance with 12-bit 2 constants. Note also that its maximum gain is higher than DAGfusion's maximum gain over ORPHEUS on every group of instances and its average gain reaches up to 17.03% on instances consisting of 6-bit 18 constants. Furthermore, it requires less CPU time than DAGfusion on instances with $n \geq 6$.

As the second experiment set, we used two benchmark sets given in [10]. Tables II-III present the results of algorithms, where *Cost*, denoting the design complexity, was computed using the 0.18- μ m standard cell library when *bwi* was 8. The results of other TCMC algorithms were taken from [10].

TABLE II. AREA ESTIMATION FOR $C = [256\ 162\ 50\ 26\ 15\ 8\ 4\ 2\ 1]$.

Method	Add	Sub	Add/Sub	MUX	Cost
[9]	0	0	1 (12-bit) 1 (14-bit)	1 (14-bit) 3-to-1 1 (16-bit) 7-to-1	4704
[8]	1 (10-bit)	1 (12-bit)	1 (10-bit) 2 (11-bit) 1 (12-bit) 1 (16-bit)	1 (8-bit) 2-to-1 1 (9-bit) 2-to-1 2 (10-bit) 2-to-1 1 (11-bit) 2-to-1 1 (12-bit) 2-to-1 1 (16-bit) 2-to-1	9578
[10]	0	0	1 (12-bit) 1 (14-bit)	1 (14-bit) 3-to-1 1 (11-bit) 4-to-1 1 (16-bit) 4-to-1	4648
ORPHEUS	1 (14-bit)	0	1 (15-bit)	1 (14-bit) 4-to-1 1 (15-bit) 6-to-1	4452

TABLE III. AREA ESTIMATION FOR $C = [362\ 392\ 473]$.

Method	Add	Sub	Add/Sub	MUX	Cost
[9]	1 (19-bit)	1 (16-bit)	1 (12-bit)	2 (12-bit) 2-to-1 1 (19-bit) 2-to-1 1 (16-bit) 3-to-1 1 (20-bit) 3-to-1	6365
[8]	1 (11-bit) 1 (12-bit) 1 (17-bit)	0	1 (11-bit)	3 (11-bit) 2-to-1 1 (14-bit) 2-to-1	5074
[10]	1 (17-bit)	1 (11-bit) 1 (12-bit) 1 (14-bit)	0	1 (14-bit) 2-to-1 1 (16-bit) 2-to-1 1 (17-bit) 2-to-1 1 (18-bit) 3-to-1	5986
ORPHEUS	1 (10-bit)	1 (15-bit) 1 (17-bit)	0	1 (11-bit) 3-to-1 1 (12-bit) 3-to-1	4036

Observe that ORPHEUS finds a TCMC design with the least complexity, where the gain over the second best solution in Tables II and III is 4.21% and 20.45%, respectively.

IV. CONCLUSIONS

This paper introduced the TCMC algorithm ORPHEUS that is equipped with efficient methods to maximize the sharing of logic operators. It was shown that it generally finds better solutions than previously proposed algorithms.

REFERENCES

- [1] R. Hartley, "Subexpression Sharing in Filters Using Canonic Signed Digit Multipliers," *IEEE TCAS-II*, vol. 43, no. 10, pp. 677–688, 1996.
- [2] I.-C. Park and H.-J. Kang, "Digital Filter Synthesis Based on Minimal Signed Digit Representation," in *DAC*, 2001, pp. 468–473.
- [3] Y. Voronenko and M. Püschel, "Multiplierless Multiple Constant Multiplication," *ACM Transactions on Algorithms*, vol. 3, no. 2, 2007.
- [4] K. Parhi, "High-Level Algorithm and Architecture Transformations for DSP Synthesis," *Journal of VLSI Signal Processing*, vol. 9, no. 1, pp. 121–143, 1995.
- [5] N. Sidahao, G. Constantinides, and P. Cheung, "Multiple Restricted Multiplication," in *FPL*, 2004, pp. 374–383.
- [6] —, "A Heuristic Approach for Multiple Restricted Multiplication," in *ISCAS*, 2005, pp. 692–695.
- [7] R. Turner and R. Woods, "Highly Efficient, Limited Range Multipliers for LUT-based FPGA Architectures," *IEEE TVLSI*, vol. 12, no. 10, pp. 1113–1117, 2004.
- [8] S. Demirsoy, I. Kale, and A. Dempster, "Reconfigurable Multiplier Constant Blocks: Structures, Algorithm and Applications," *Springer CSSP*, vol. 26, no. 6, pp. 793–827, 2007.
- [9] P. Tummeltshammer, J. Hoe, and M. Püschel, "Time-Multiplexed Multiple-Constant Multiplication," *IEEE TCAD*, vol. 26, no. 9, pp. 1551–1563, 2007.
- [10] J. Chen and C.-C. Chang, "High-Level Synthesis Algorithm for the Design of Reconfigurable Constant Multiplier," *IEEE TCAD*, vol. 28, no. 12, pp. 1844–1856, 2009.
- [11] O. Gustafsson, A. Dempster, and L. Wanhammar, "Extended Results for Minimum-adder Constant Integer Multipliers," in *ISCAS*, 2002, pp. 73–76.
- [12] P. Barth, "A Davis-Putnam Based Enumeration Algorithm for Linear Pseudo-Boolean Optimization," Max-Planck-Institut Fur Informatik, Tech. Rep., 1995.